

Oviedo V Postgraduate Meeting On Theoretical Physics

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Neutron star structure r_* $ds^{2} = -e^{\nu(r)}dt^{2} + e^{\lambda(r)}dr^{2} + r^{2}d\Omega_{2}$ $T_0^{\ 0} = \varepsilon(r) \quad T_i^{\ j} = P(r)\delta_i^j \qquad P(r_*) = 0$ $R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = 8 \pi G T_{\mu\nu}$ $\partial_{\mu} T^{\mu}_{\nu} = 0$ Tolman–Oppenheimer–Volkoff equations Only unknown: Equation of State $F(\varepsilon, P) = 0$



QCD phase diagram

Perturbation Theory $\mu > 1 \ GeV$ $\mu < 500 \ MeV$ Lattice QCD $\mu \ll T$ $T \sim 0.1 - 1 \ keV$ Chiral Perturbation Theory $n \le n_s \simeq 0.16 \ fm^{-3} \ n \sim 5 \ n_s$

Phenomenological models: Nambu-Jona-Lasinio, Walecka Extrapolated from low density







Strong coupling

No problems with large density

Large-N: baryons are difficult

Not QCD: systematic uncertainty

0 0

Strong coupling

No problems with large density

Alternative large-N limits

Not QCD: systematic uncertainty 🕟

Strong coupling

No problems with large density

Restrict to deconfined phase

Not QCD: systematic uncertainty 🕟

No problems with large density

Strong coupling

Restrict to deconfined phase

universality in quark-gluon plasma (?)



Quick introduction to AdS/CFT

Basics

AdS UV/IR Black holes



AdS space



d dimensions



AdS space radial direction Field theory directions

volume ~ area



AdS space

length = length

infinite distance







Holography

UV CFT



Black hole

Thermal state

Temperature = Hawking temperature

Thermal Entropy = Black hole area

$$ds^{2} = \frac{dr^{2}}{f(r)r^{2}} + r^{2}(-f(r)dt^{2} + \delta_{ij}dx^{i}dx^{j})$$
$$f(r) = 1 - \frac{r_{H}^{d}}{r^{d}}$$



Black hole

Thermal state

Temperature ~ r_H Thermal Entropy ~ r_H^{d-1}

$$ds^{2} = \frac{dr^{2}}{f(r)r^{2}} + r^{2}(-f(r)dt^{2} + g_{ij}dx^{i}dx^{j})$$
$$f(r) = 1 - \frac{r_{H}^{d}}{r^{d}}$$

The correspondence

Symmetries Fields/Operators Action



Field theory

<u>Gravity</u>

Local symmetries are not ``physical"

Global symmetries \longrightarrow Asymptotic symmetries Conformal symmetries \longrightarrow AdS isometries dr^2

$$r \rightarrow \lambda r \qquad x^{\mu} \rightarrow x^{\mu}/\lambda \qquad ds^2 = \frac{dr^2}{r^2} + r^2 \eta_{\mu\nu} dx^{\mu} dx^{\nu}$$

Operators/Fields



Local gauge-invariantLocal fields $\mathcal{O}(x)$ $\Phi(x,r)$

Conformal dimension Δ Mass $M_s^2 = \Delta(\Delta - d)$

Equal charges and spin

$$\Phi(x,r) \sim \frac{g}{r^{d-\Delta}} + \frac{\langle \mathcal{O} \rangle}{r^{\Delta}}$$



<u>Field theory</u>

<u>Gravity</u>

Generating functional
On-Shell action

$$W[g] = \left\langle e^{\int g \,\mathcal{O}} \right\rangle \qquad S[g] = \frac{1}{16 \,\pi G} \int (R + \mathcal{L}_{matter})$$
$$\left\langle \mathcal{O}\mathcal{O} \right\rangle = \frac{\delta^2 \, W}{\delta \, g^2}$$

A model of deconfined matter

Field theory

 $\mathcal{N}_c \to \infty$ $\mathcal{N} = 4 \text{ SU}(N_c)$ Super Yang-Mills $\lambda_{YM} = g_{YM}^2 N_c \gg 1$

 $\mathcal{N} = 2$ $N_f \ll N_c$ Flavor hypermultiplets

Fields in adjoint of color: A_{μ} , $\phi^{i=1,\dots,6}$, $\lambda^{a=1,\dots,4}$ Fields in (anti)fundamental of color: $q, \tilde{q}, \psi, \tilde{\psi}$

Gravity dual

 $AdS_5 \times S^5 + N_f$ D7 flavor branes



Gravity dual

 $AdS_5 \times S^5 + N_f$ D7 flavor branes

$$S_{D7} = -T_7 \int e^{-\varphi} \sqrt{\det(g_{ab} + F_{ab})} + T_7 \int C_4 \wedge F \wedge F$$

$$A_0 \approx \mu + \frac{\langle J^0 \rangle}{r^2} \qquad \text{baryon chemical potential}$$

$$baryon charge density$$

(beta-equilibrium: no electrons)

Free energy

free energy = -on-shell action (gravity+D7)

gravity action does not depend on chemical potential

$$\mathcal{F}_G \sim -N_c^2 T^4$$

D7 brane action at small temperatures

$$\mathcal{F}_{D7} = -\frac{N_c N_f}{4\gamma^3 \lambda_{YM}} \left(\mu^2 - \mu_0^2\right)^2 + O(\mu^3 T)$$

[Karch, O'Bannon 0709.0570]

Extrapolation to QCD

Number of color and flavors the same as QCD $N_c = N_f = 3$

Stefan-Boltzmann result at large chemical potentials

$$\mathcal{F}_{D7} \simeq -\frac{N_c N_f}{4\gamma^3 \lambda_{YM}} \mu^4 = -\frac{N_c N_f}{12 \pi^2} \mu^4 \qquad \lambda_{YM} = \frac{3 \pi^2}{\gamma^3} \simeq 10.74$$

Pressure (=- free energy) vanishes ~ 1/3 nucleon mass

 $\mu_0 \simeq 308.55 \, MeV$

Application to neutron stars

Comparison to nuclear matter



first order phase transition





deconfined matter at the core starts





The importance of being stiff

A non-Trivial Condition for Serious EoS

Neutron star mass larger for stiffer EoS



stiffness ~ speed of sound

 $\frac{\partial P}{\partial \varepsilon}$

<u>Conjecture</u>: speed of sound is bounded in holographic models



[Cherman, Cohen, Nellore '09; Hohler, Stephanov '09] [Cherman, Nellore '09]

Assumptions: UV fixed point (asymptotically AdS)

Shown true for: scalars at finite temperature Holds in SUGRA models: Klebanov-Strassler, N=2* Holds in D-brane models even at finite density (D7 model)

EoS of nuclear matter models







<u>Conjecture</u>: speed of sound is bounded in holographic models



Assumptions: UV fixed point (asymptotically AdS)

scalar at low temperature and finite density small breaking of conformal invariance SUGRA model: R-charged black hole

<u>Conjecture</u>: speed of sound is bounded in holographic models



Outlook

Speed of sound with large breaking of conformal invariance

Mixed phases in neutron stars

Nuclear matter in holographic models (light baryons?)

Surface tension of bubbles in mixed phases

Transport properties, emissivities, etc

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