

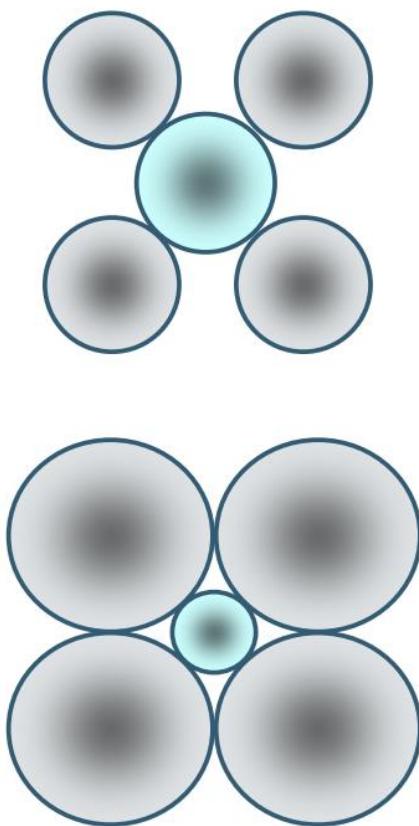
# **INSERCIONES OCTAEDRICAS Y TETRAEDRICAS EN REDES FCC Y BCC**

# **INSERCIÓNES OCTAEDRICAS Y TETRAEDRICAS EN REDES FCC Y BCC**

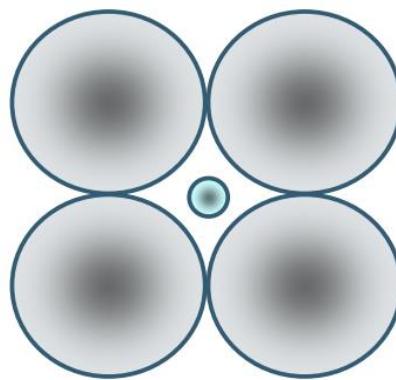
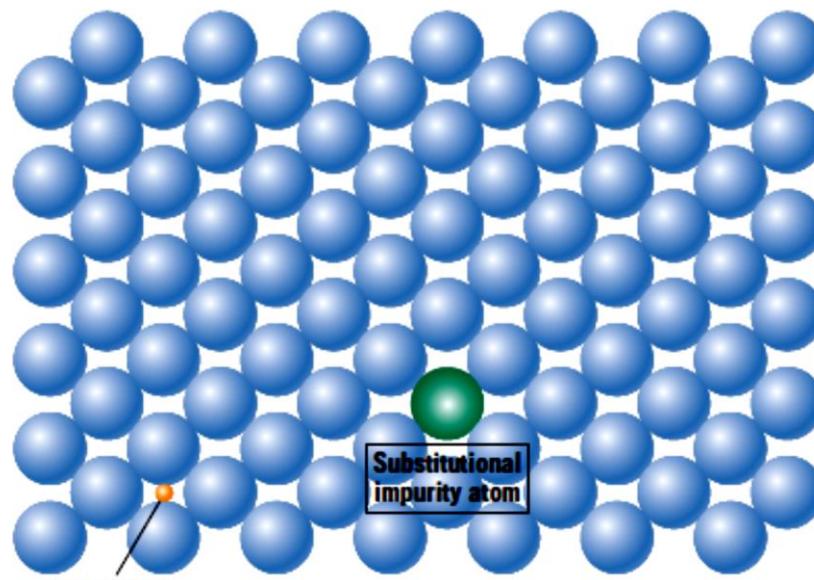
## **REFERENCIA BIBLIOGRÁFICA:**

- Pp. 110 – 114 “**CIENCIA E INGENIERIA DE MATERIALES**”. Prof. José Antonio Pero-Sanz Elorz

# ATOMOS INTERSTICIALES Y DE SUSTITUCION

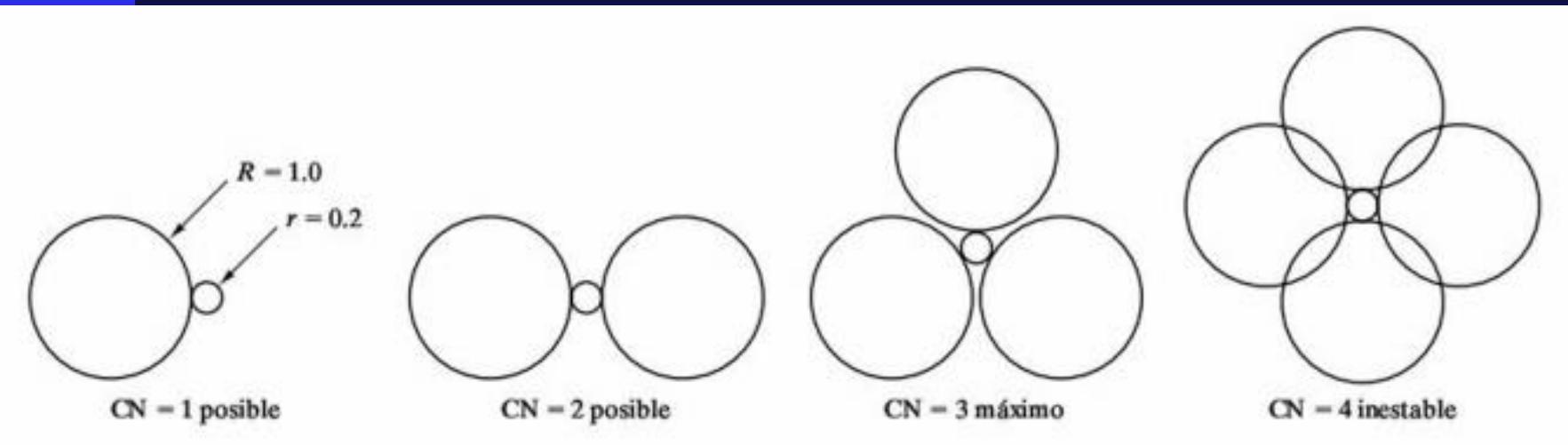


Estables



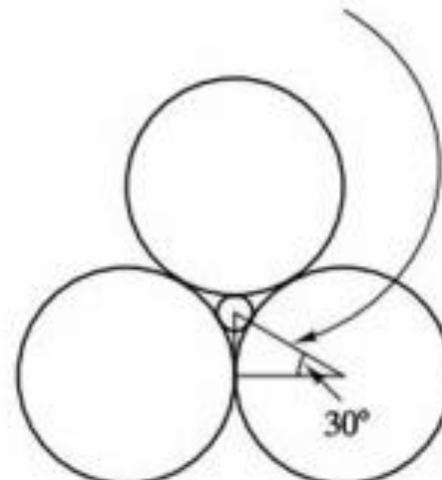
Inestable

# Coordinación entre compuestos iónicos: $r_i/r_s = 0,2$



Relación  $(r_i/r_s)_{\min}$  para una coordinación 3

$$\cos 30^\circ = 0.866 = \frac{R}{r+R} \rightarrow \frac{r}{R} = 0.155$$



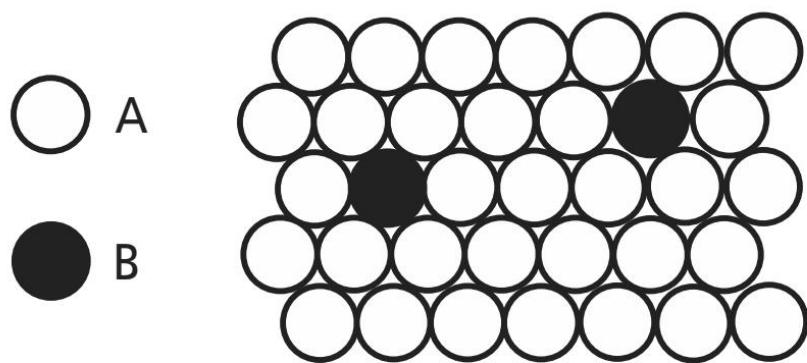


Schéma à deux dimensions  
d'une solution solide de substitution de B dans A.

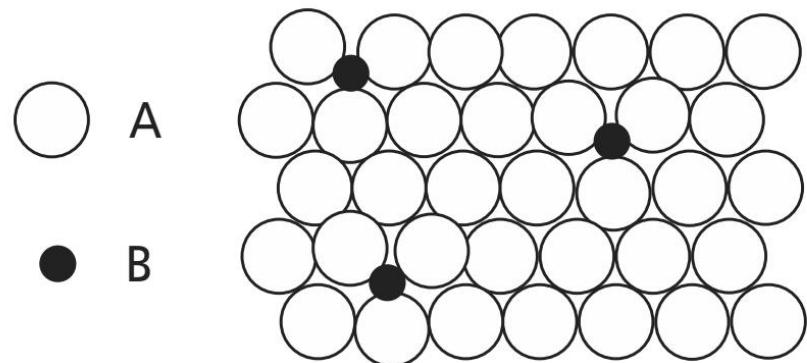
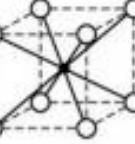
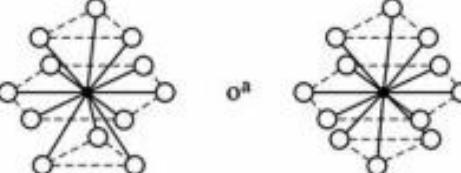


Schéma à deux dimensions  
d'une solution solide d'insertion de B dans A.

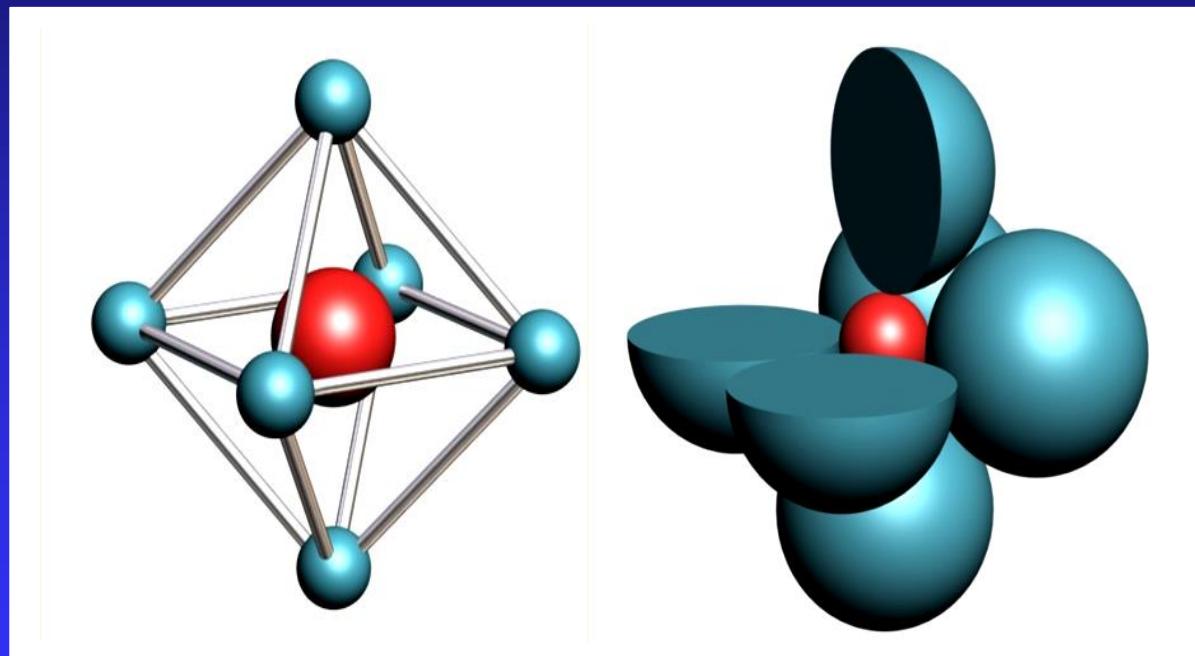
$$\frac{a - a_0}{a_0} = x_B \frac{r_B - r_A}{r_A}$$

# Relación de radios anión-catión para huecos

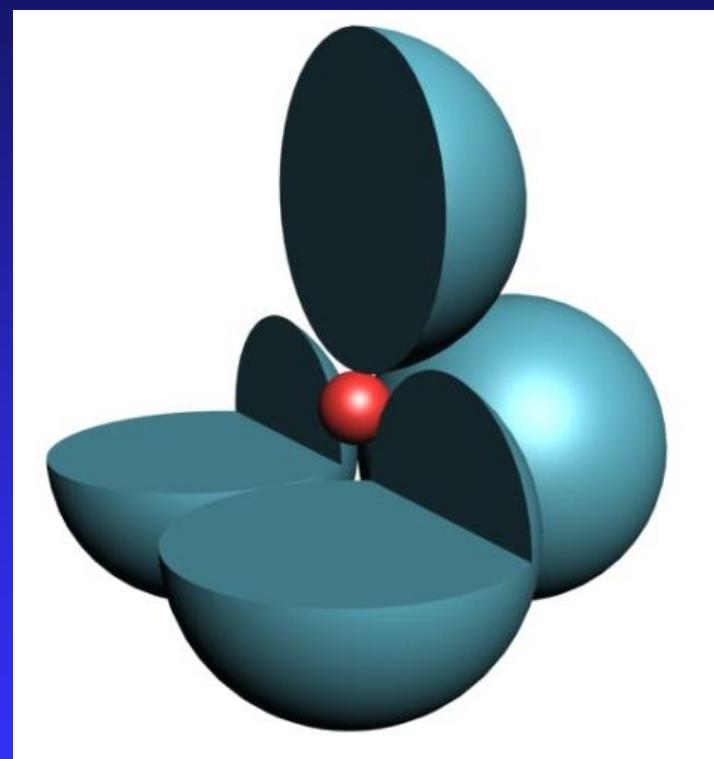
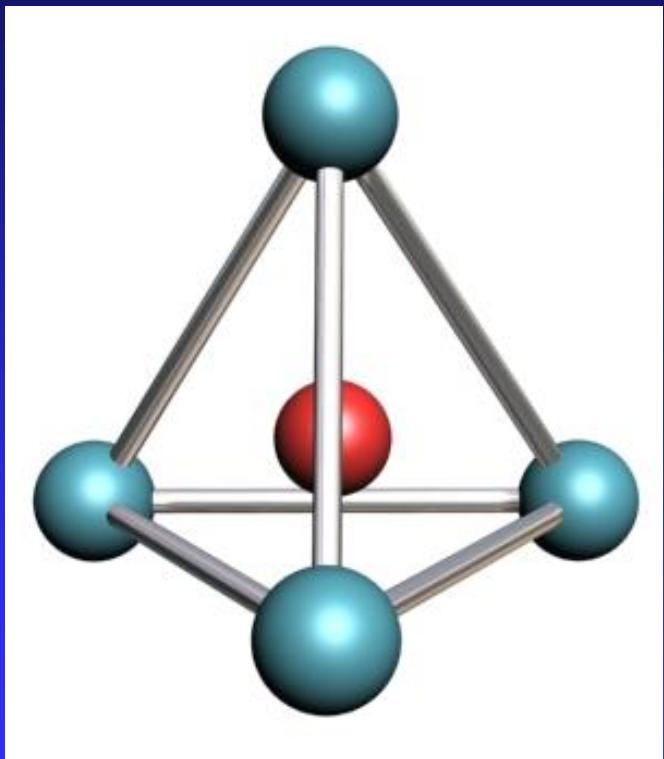
Número de coordinación	Relación entre radios $r/R$	Geometría de coordinación
2	$0 < \frac{r}{R} < 0.155$	
3	$0.155 \leq \frac{r}{R} < 0.225$	
4	$0.225 \leq \frac{r}{R} < 0.414$	
6	$0.414 \leq \frac{r}{R} < 0.732$	
8	$0.732 \leq \frac{r}{R} < 1$	
12	1	

\* La geometría de la izquierda corresponde a la estructura hexagonal compacta (hcp), y la de la derecha a la estructura cúbica centrada en las caras (fcc). Estas estructuras cristalinas se verán en el Capítulo 3.

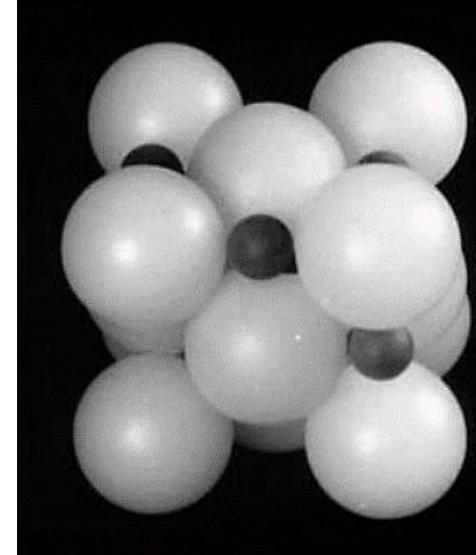
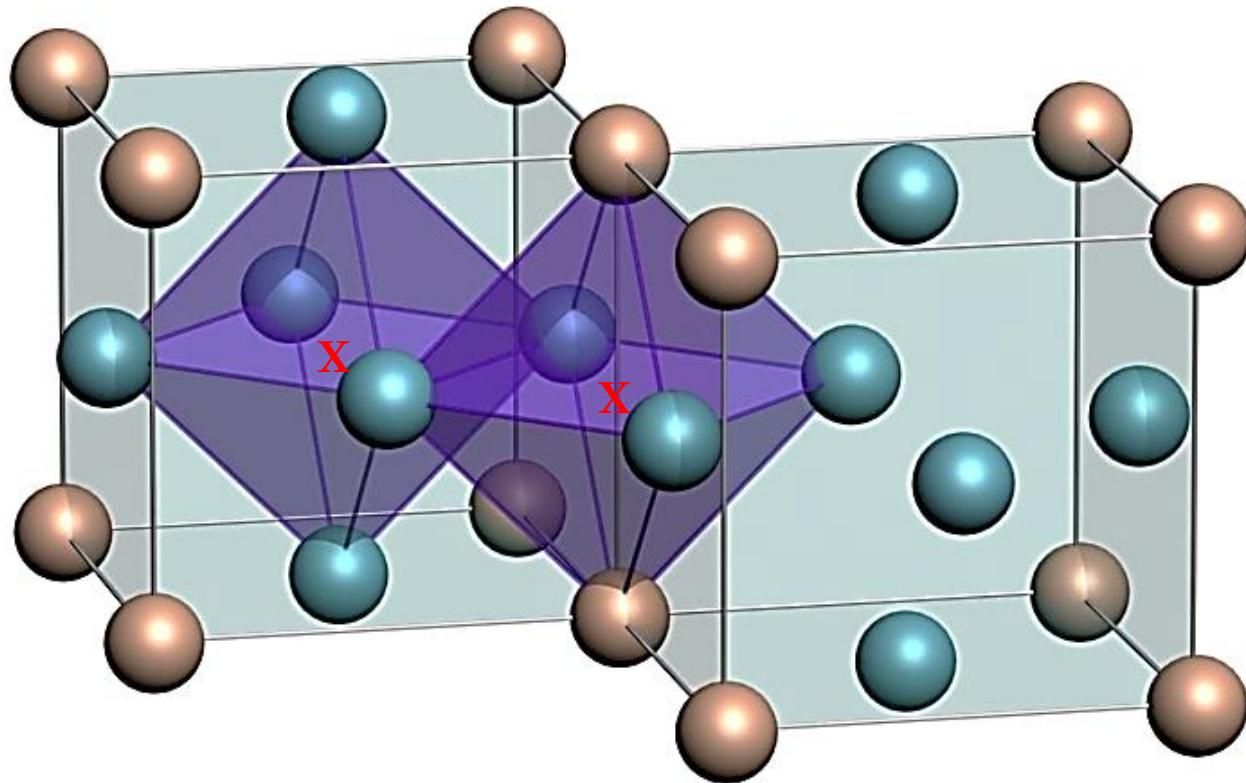
# INSERCIIONES OCTAEDRICAS



# Huecos tetraédricos



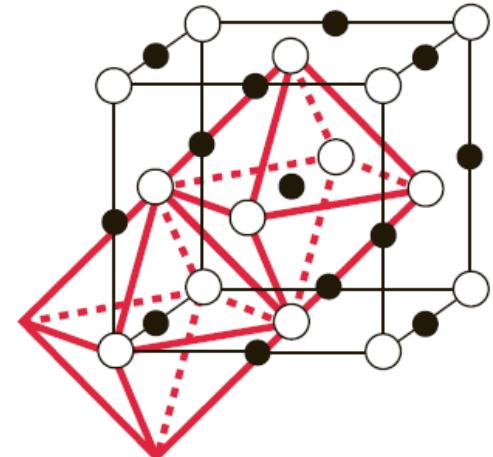
# Sistema FCC: Huecos octaédricos



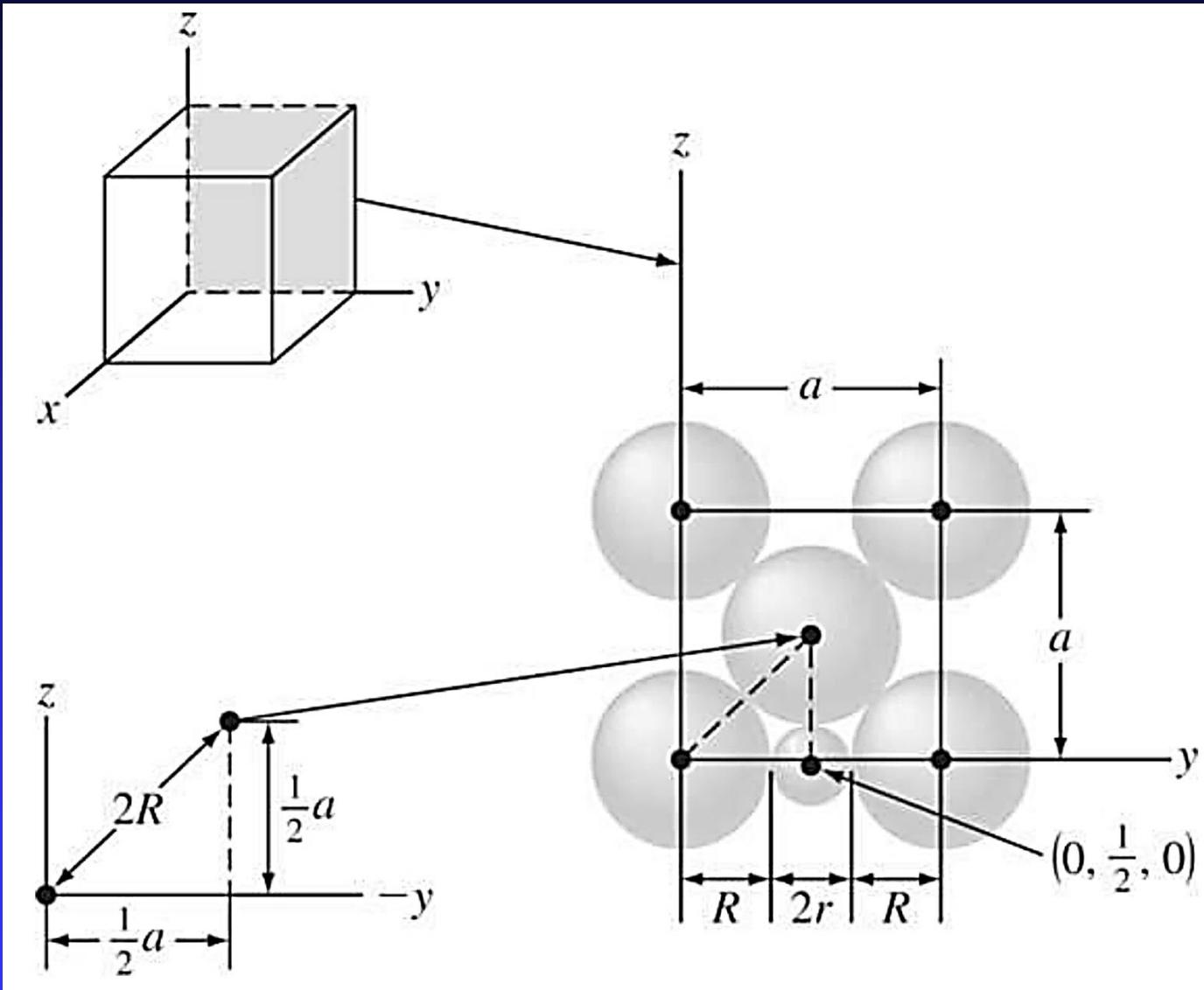
Aristas:  $12 / 4 \text{ celdas} = 3 \text{ huecos / celda}$

Centro celda = 1 hueco / celda

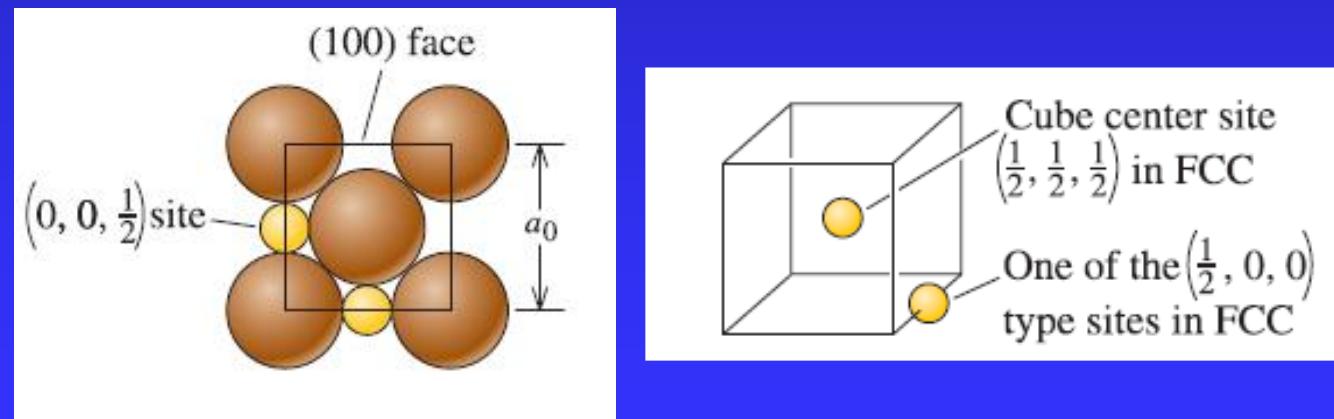
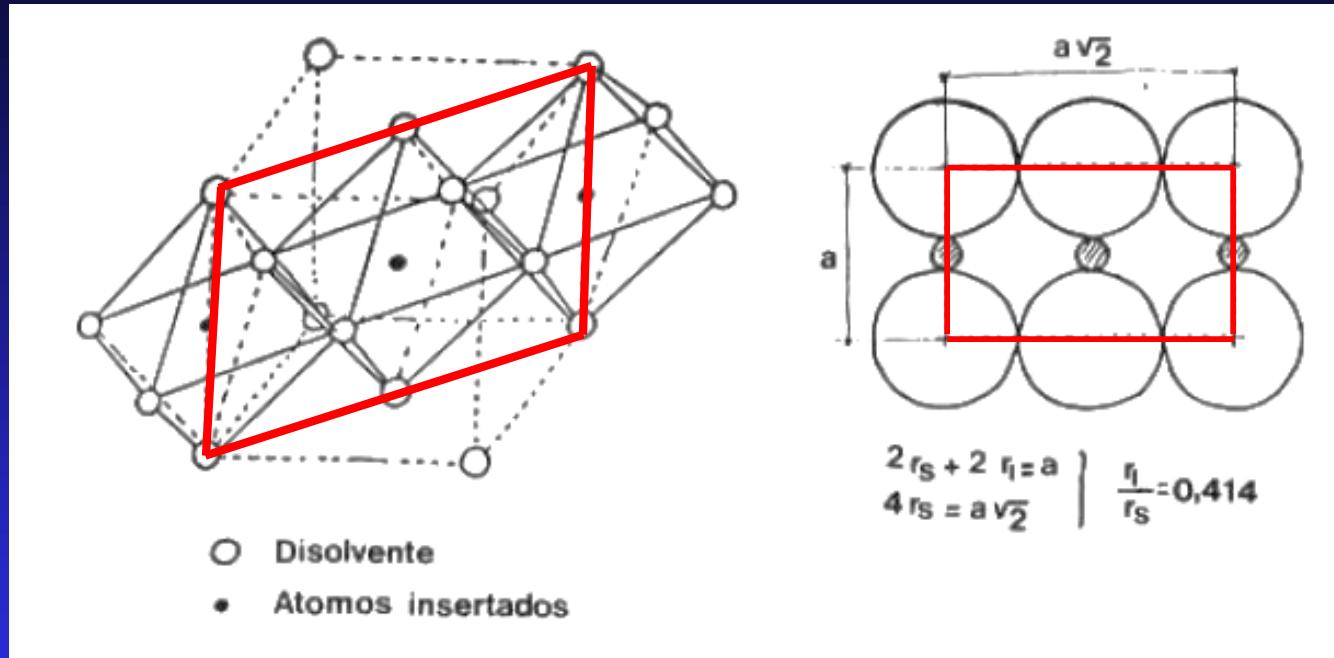
**ATOMOS INSERTADOS = 4 átomos/celda**



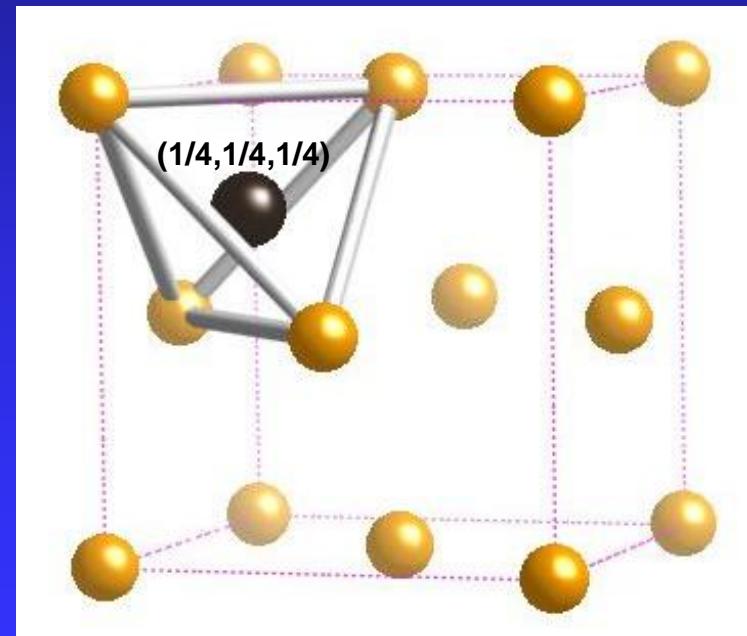
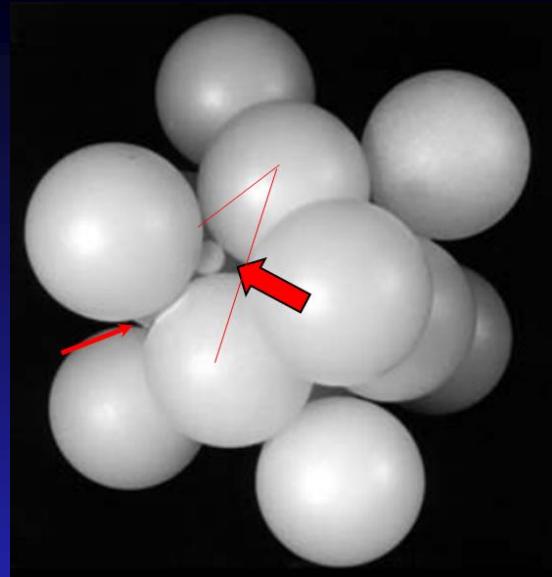
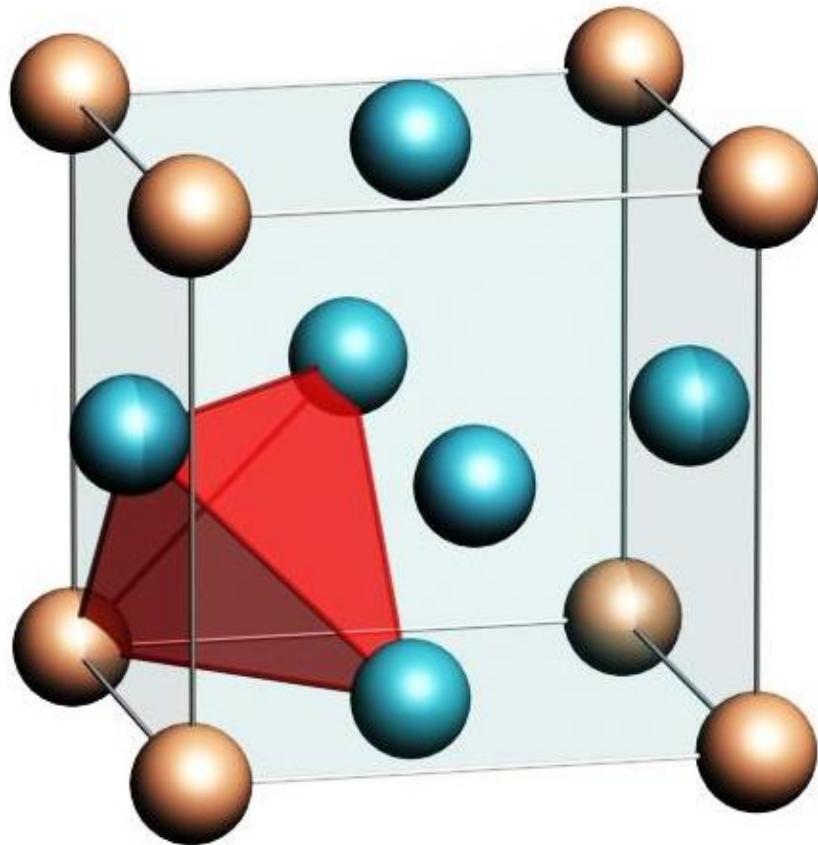
# Sistema FCC: Inserción octaédrica



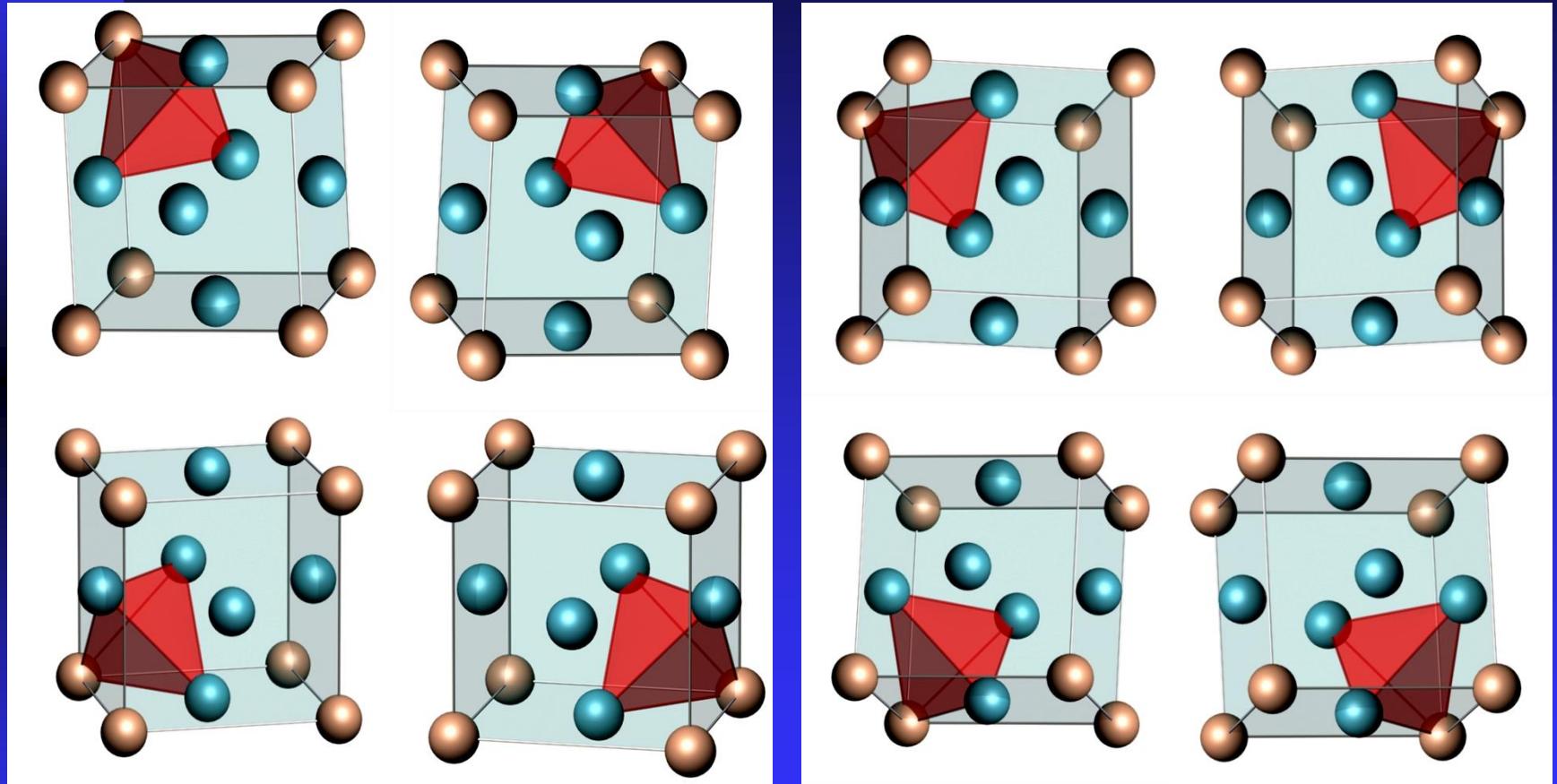
# FCC. Huecos octaédricos: $r_i/r_s$



# Sistema FCC: Huecos tetraédricos

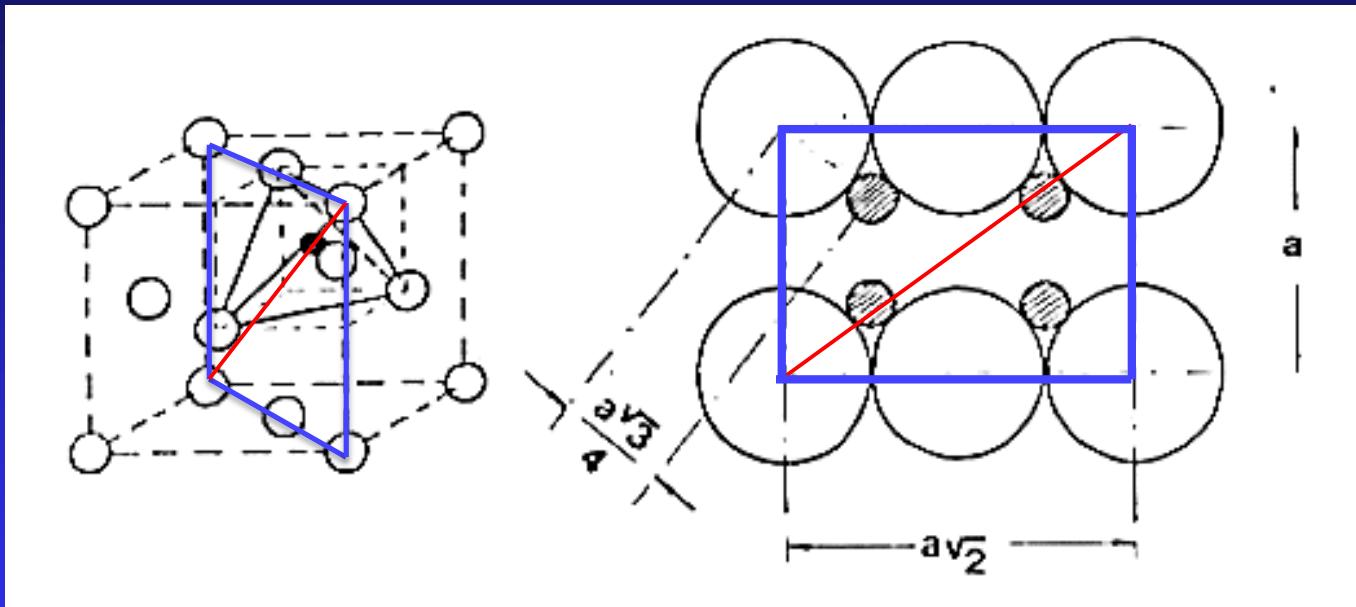


# FCC: Huecos tetraédricos (8 huecos/celda)



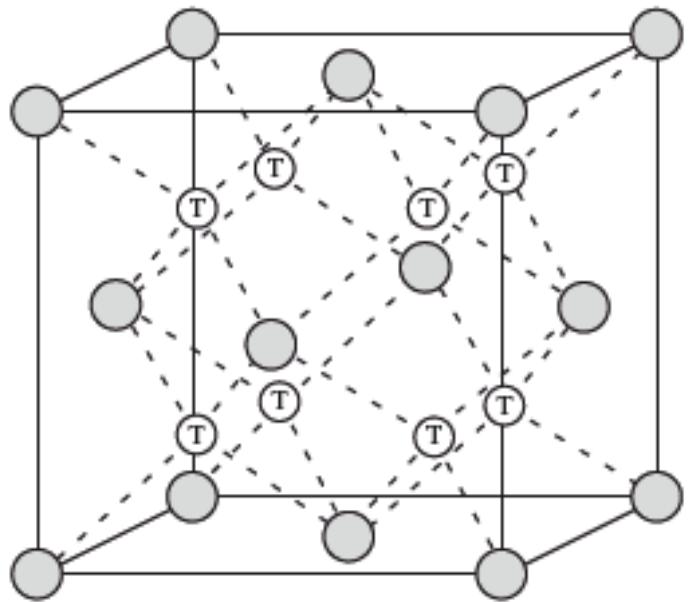
Huecos internos, dentro de la celda

# FCC. Huecos tetraédricos: $r_i/r_s$



$$2 r_s = \frac{a\sqrt{2}}{2} \quad r_s + r_i = \frac{a\sqrt{3}}{4}$$

$$\frac{r_i}{r_s} = \frac{a\sqrt{3}/4}{a\sqrt{2}/4} - 1 = 0,225$$

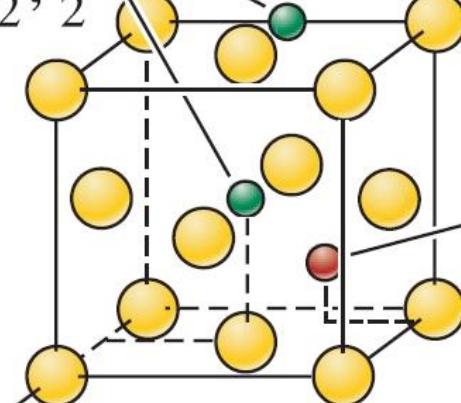


## Sistema FCC: Inserciones tetraédricas y octaédricas

Huecos tetraédricos  $\Rightarrow$  8 átomos/celda

Octahedral

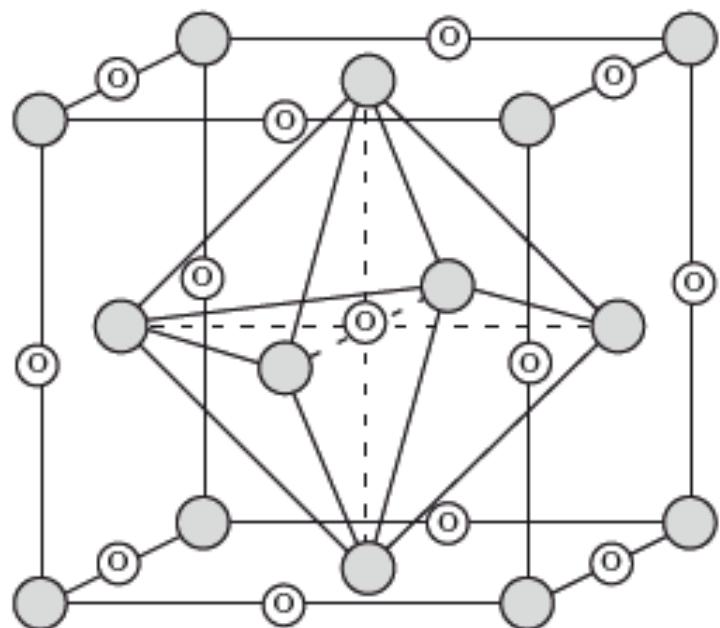
$\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$        $0, \frac{1}{2}, 1$



Tetrahedral

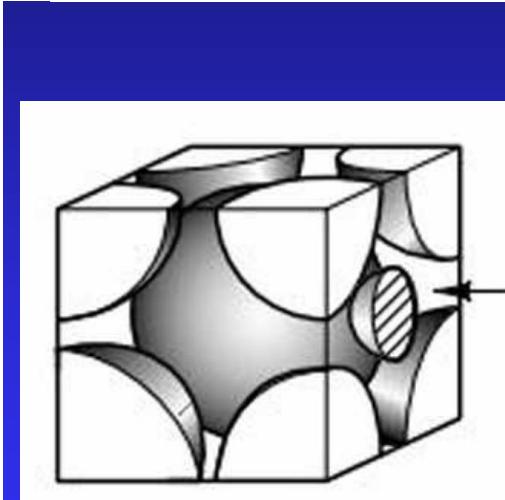
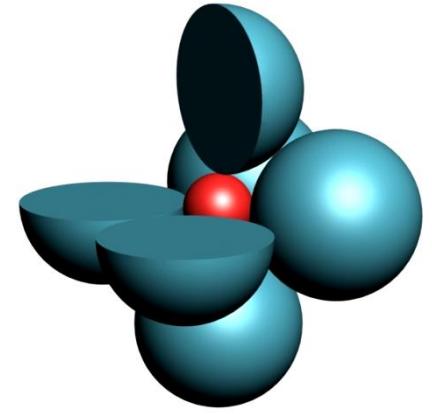
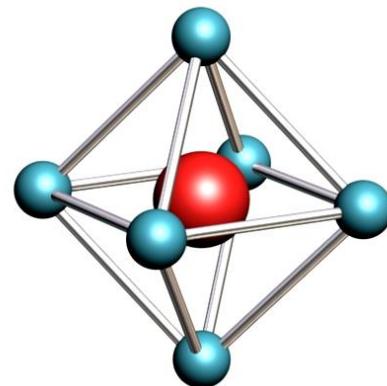
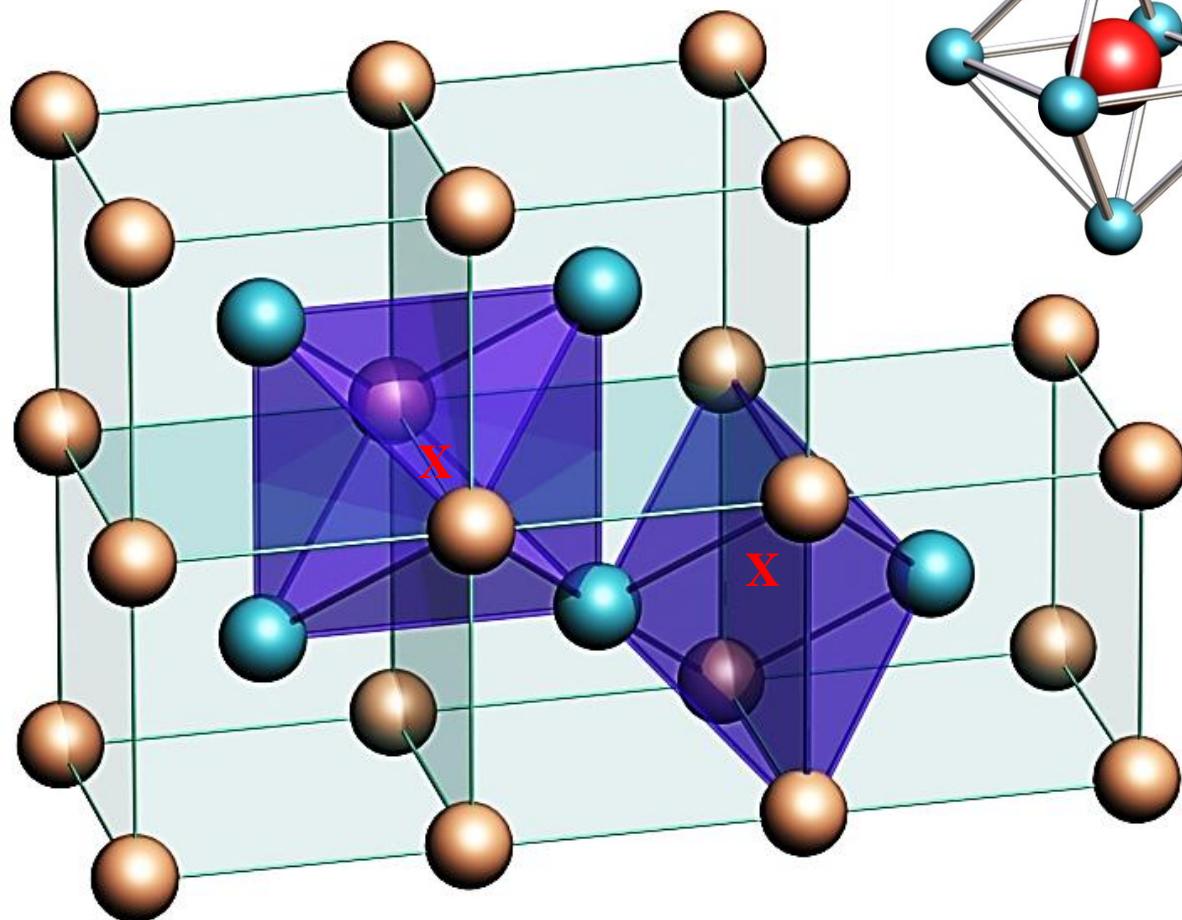
$\frac{1}{4}, \frac{3}{4}, \frac{1}{4}$

FCC



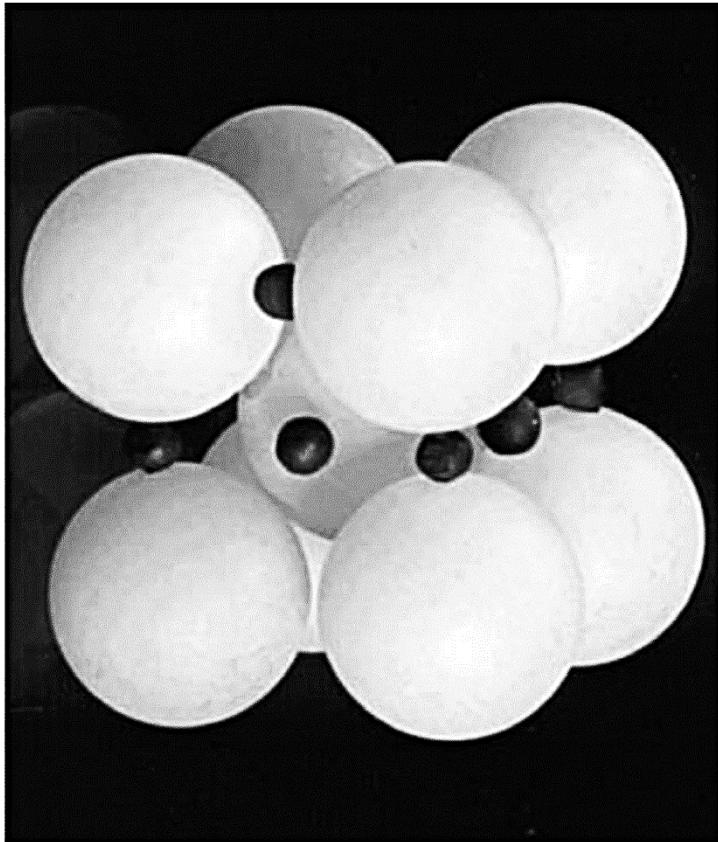
Huecos octaédricos  $\Rightarrow$  4 átomos/celda

# Sistema BCC: Huecos octaédricos

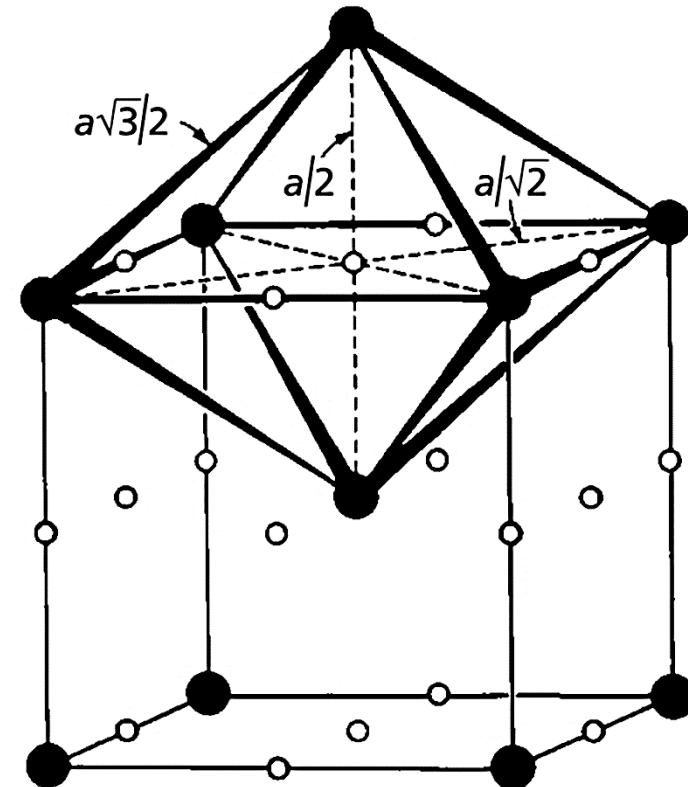


$$(12 \text{ aristas} / 4 \text{ celdas}) + (6 \text{ caras} / 2 \text{ celdas}) = \mathbf{6 \text{ huecos} / \text{celda}}$$

# Sistema BCC: Huecos octaédricos



(a)



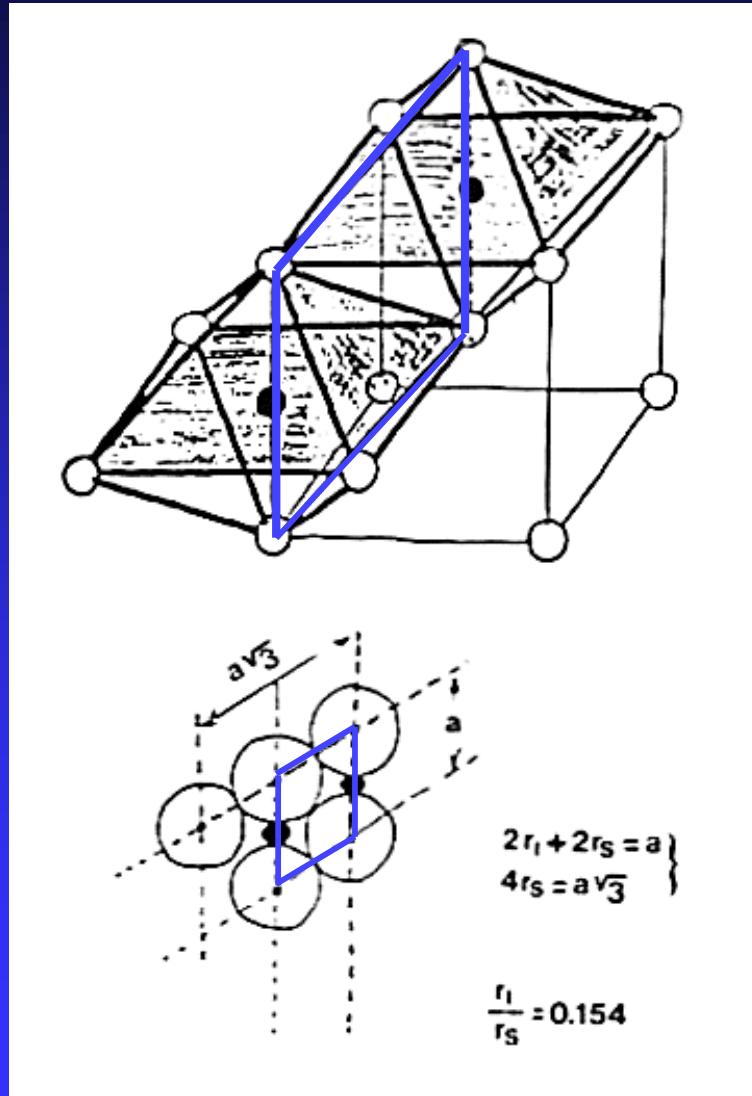
(b) ● Metal atoms  
○ Octahedral interstices

$(6 \text{ huecos / caras} / 2 \text{ celdas}) \Rightarrow 3 \text{ átomos / celda}$

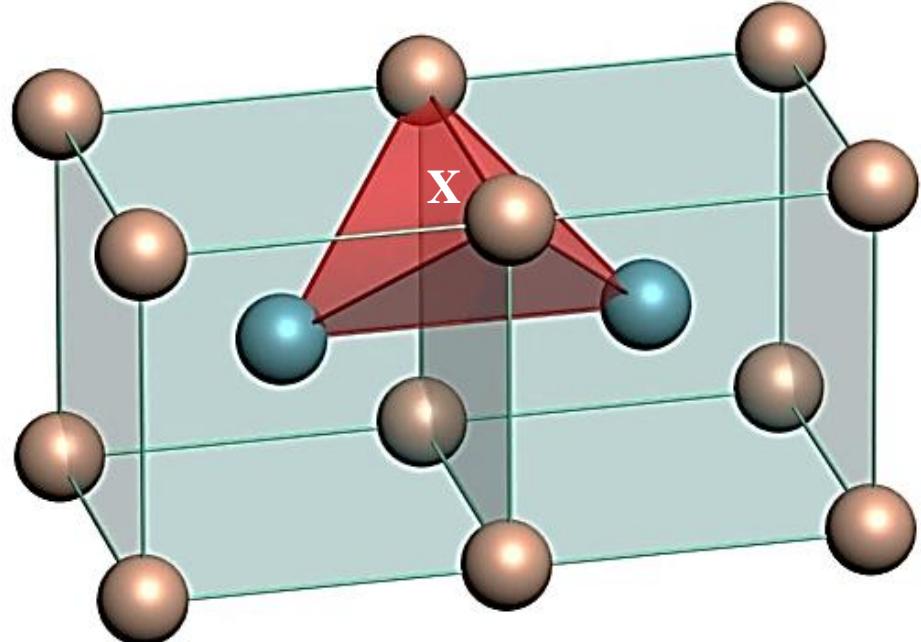
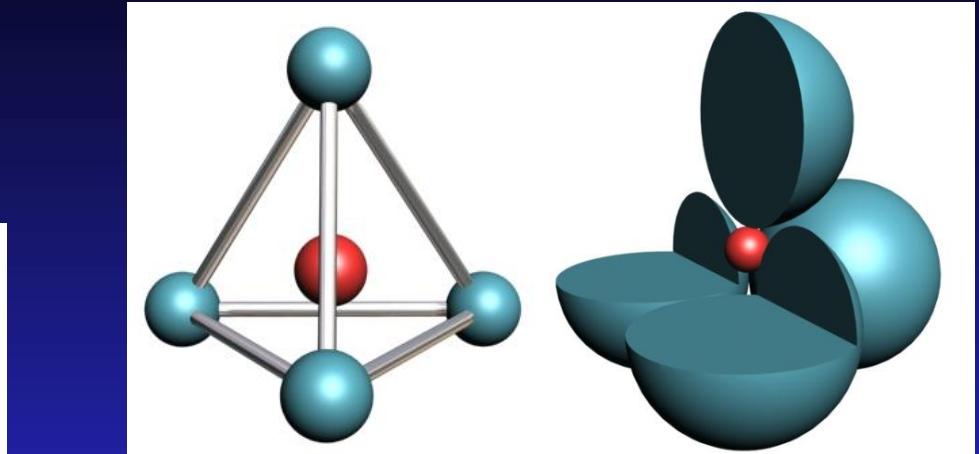
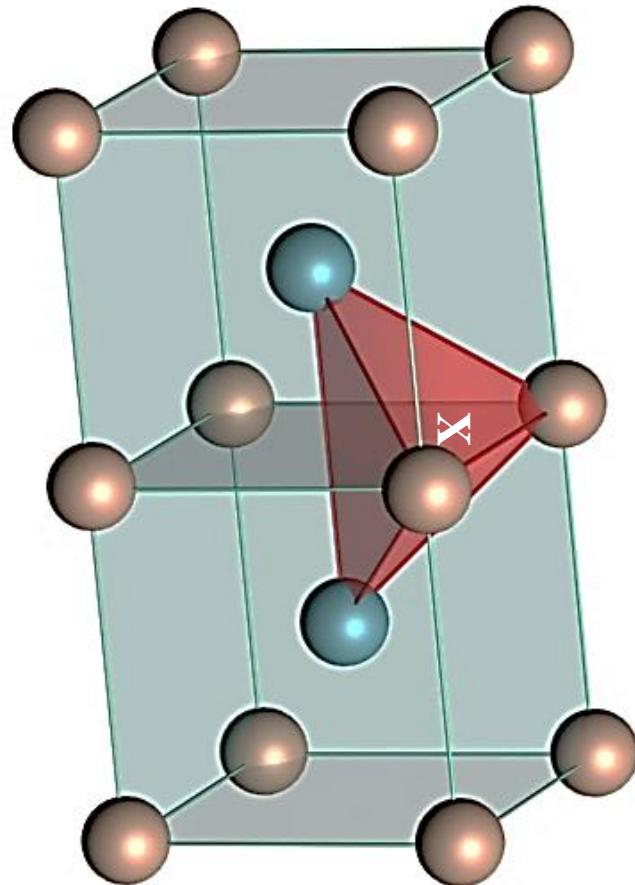
$(12 \text{ huecos / caras} / 4 \text{ celdas}) \Rightarrow 3 \text{ átomos / celda}$

**6 átomos/celda**

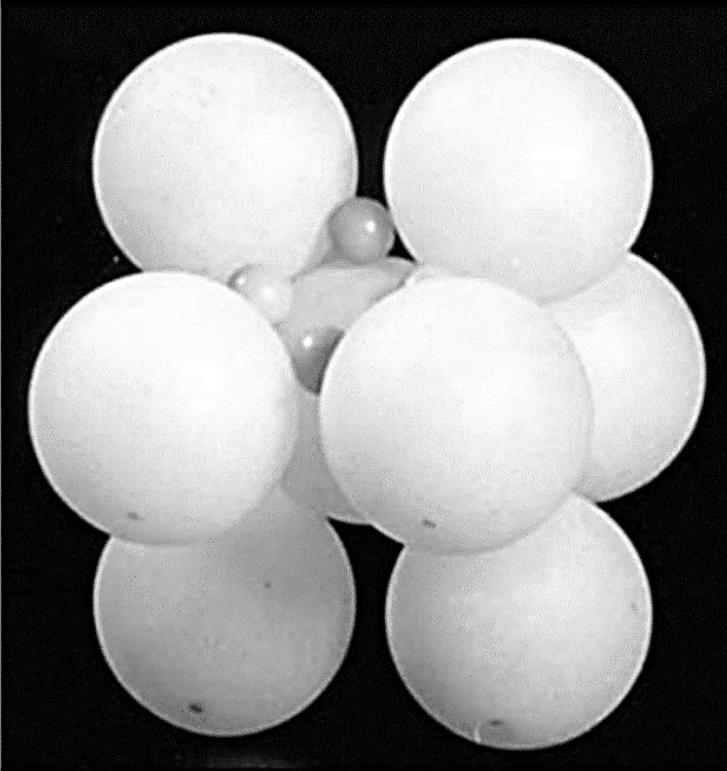
# BCC. Huecos octaédricos: $r_i/r_s$



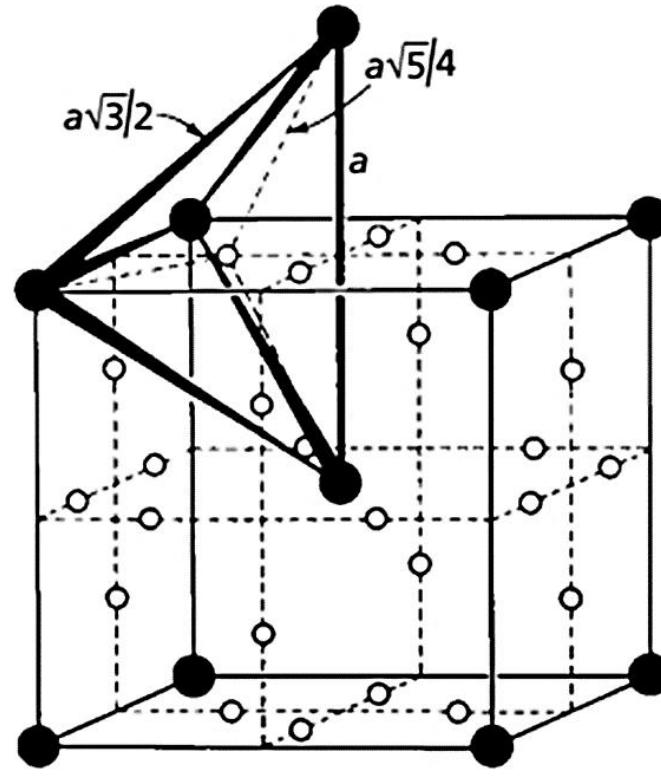
# Sistema BCC: Huecos tetraédricos



# Sistema BCC: Huecos tetraédricos



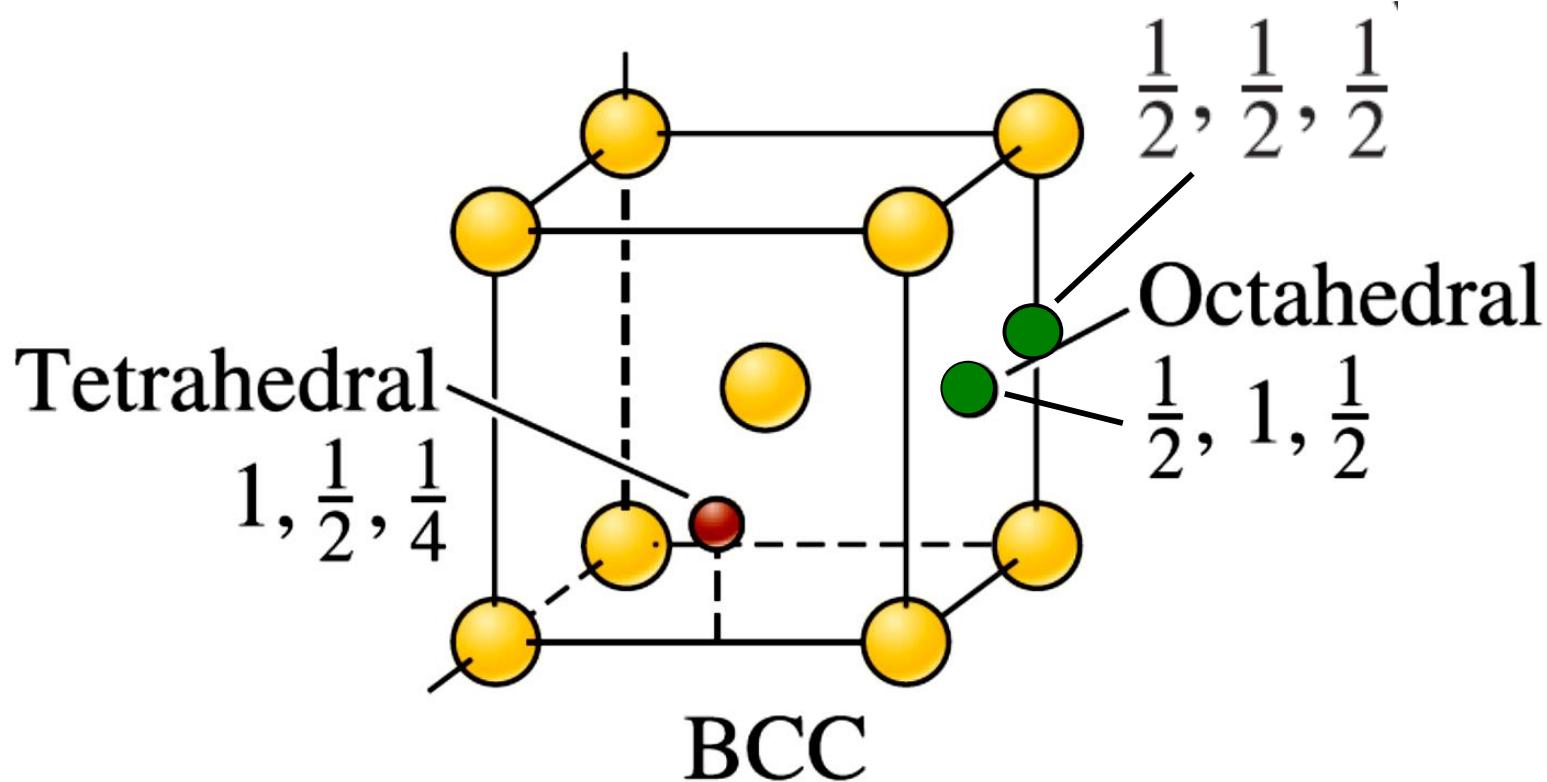
(c)



(d) ● Metal atoms  
○ Tetrahedral interstices

6 caras (4 huecos / 2 celdas)  $\Rightarrow$  12 átomos / celda

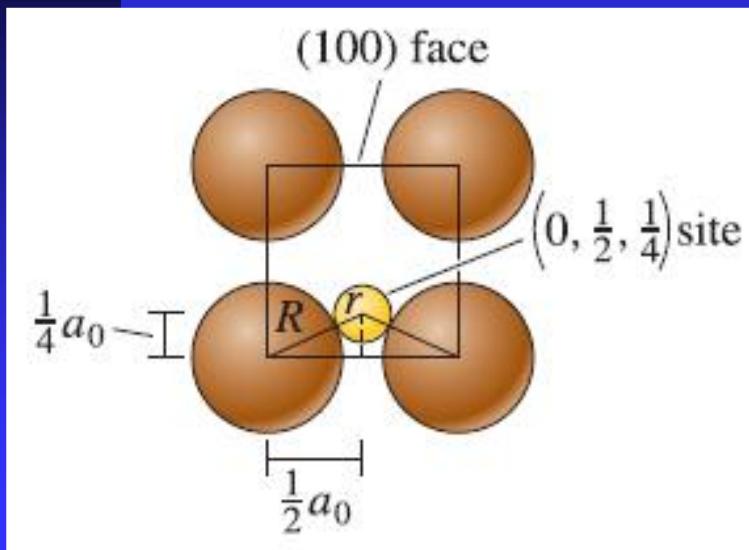
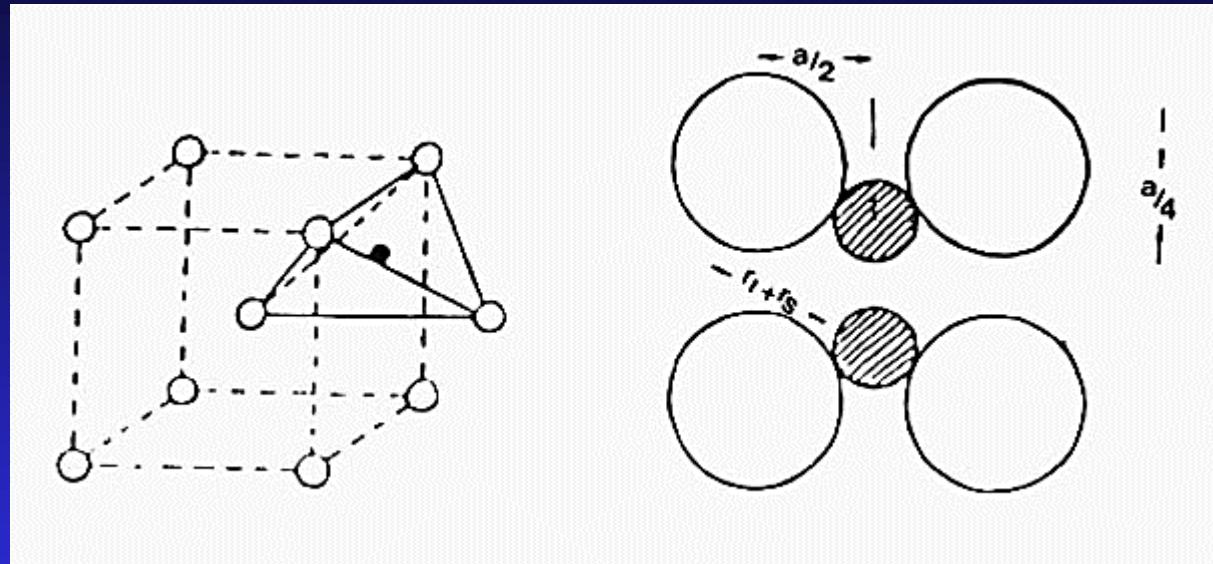
# Sistema BCC: Inserciones tetraédricas y octaédricas



Huecos tetraédricos  $\Rightarrow$  12 átomos

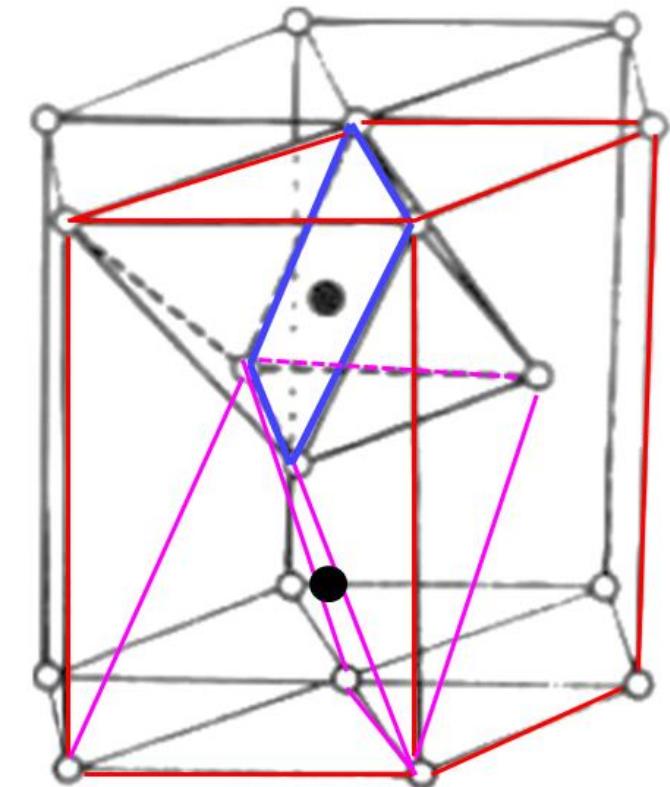
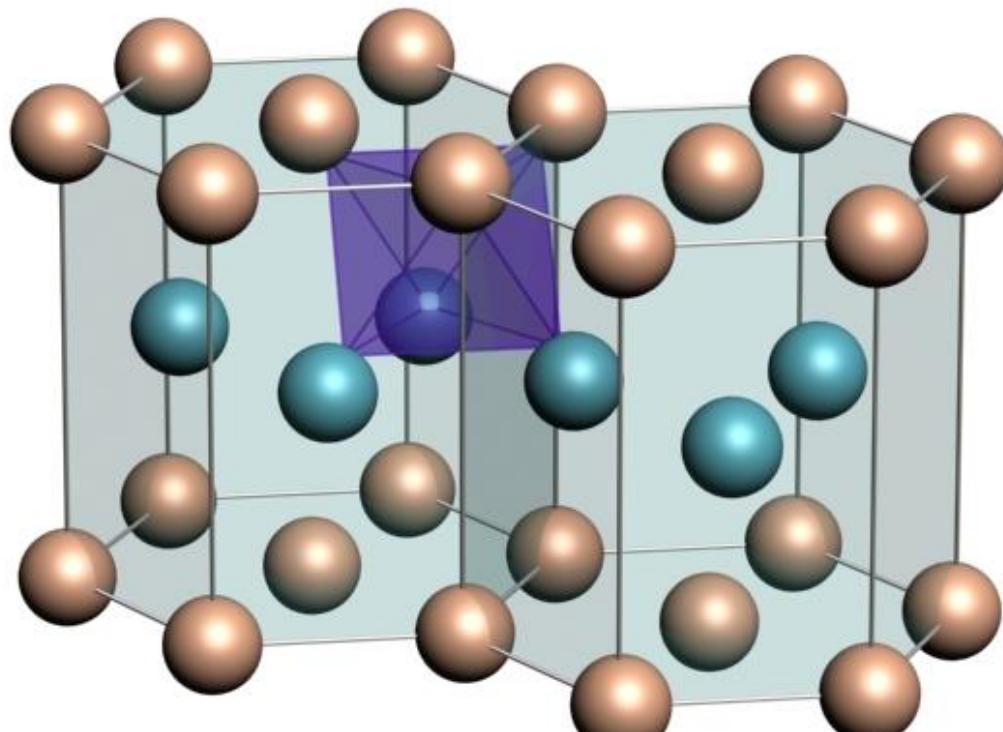
Huecos octaédricos  $\Rightarrow$  6 átomos

# Sistema BCC: Huecos tetraédricos



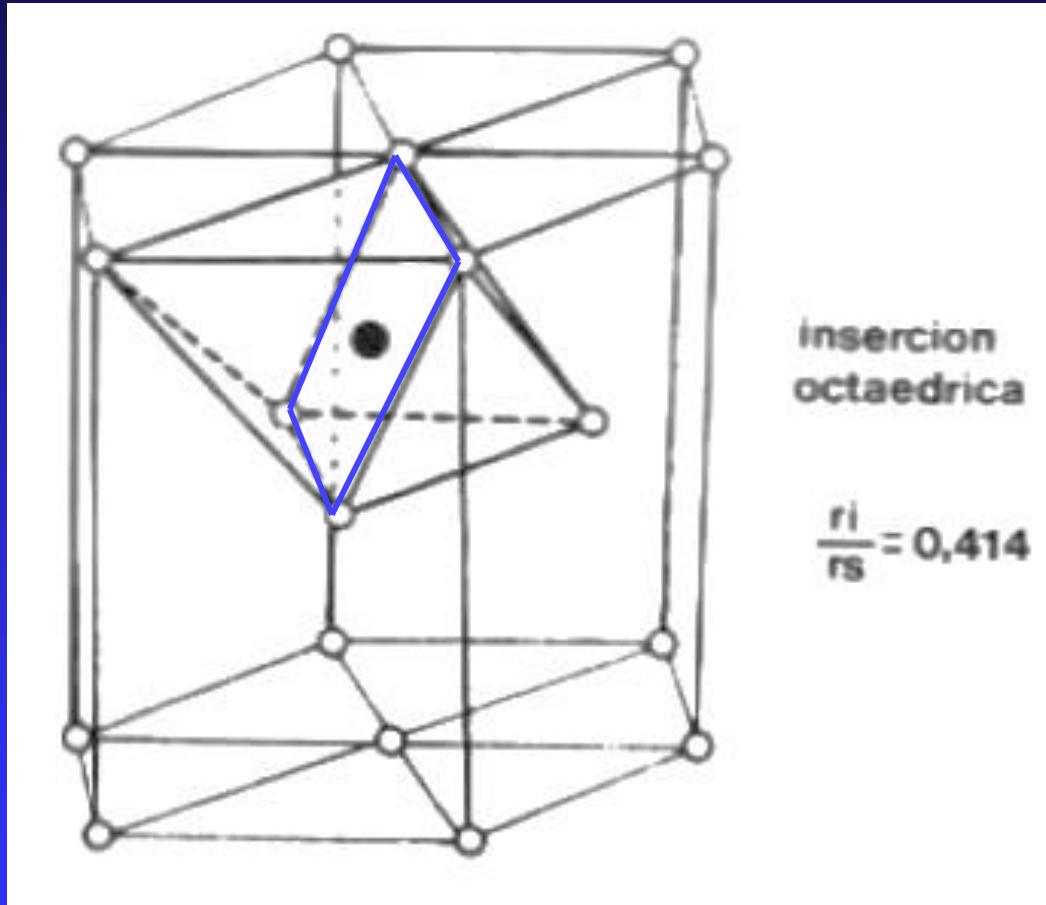
$$\left. \begin{aligned} (r_1 + r_s)^2 &= \frac{a^2}{4} + \frac{a^2}{16} \rightarrow r_1 + r_s = \frac{a\sqrt{5}}{4} \\ 4r_s &= a\sqrt{3} \end{aligned} \right\} r_1/r_s = 0.291$$

# SISTEMA HC: Huecos octaédricos

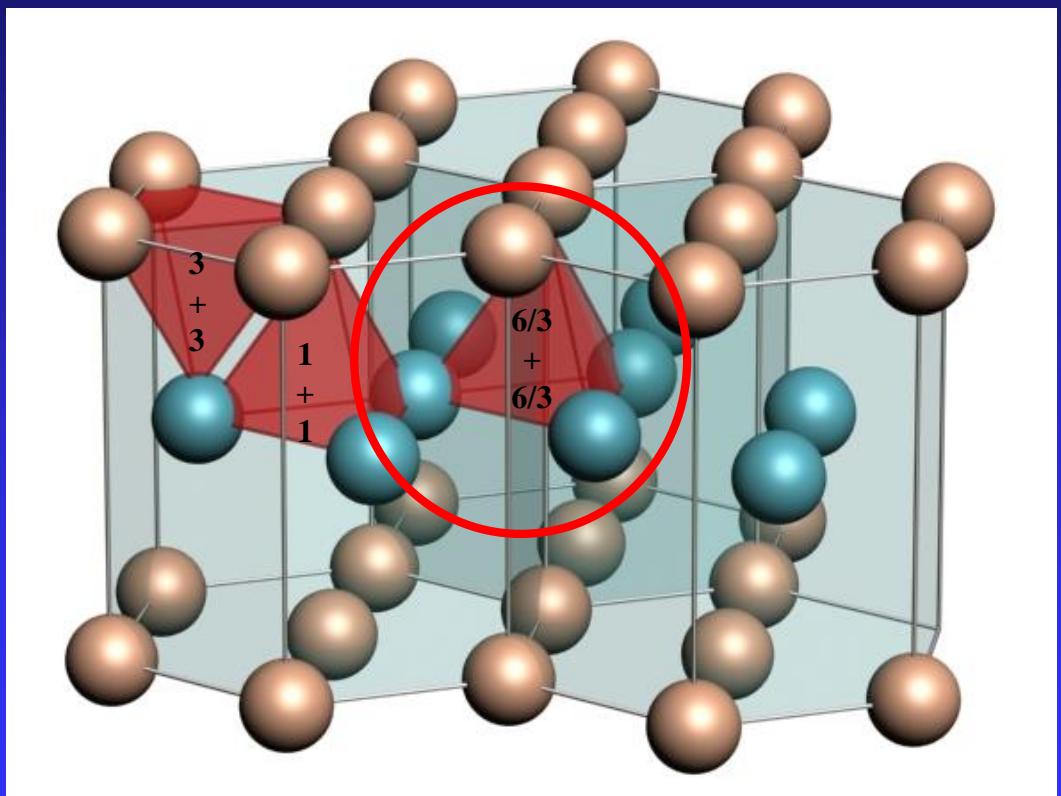
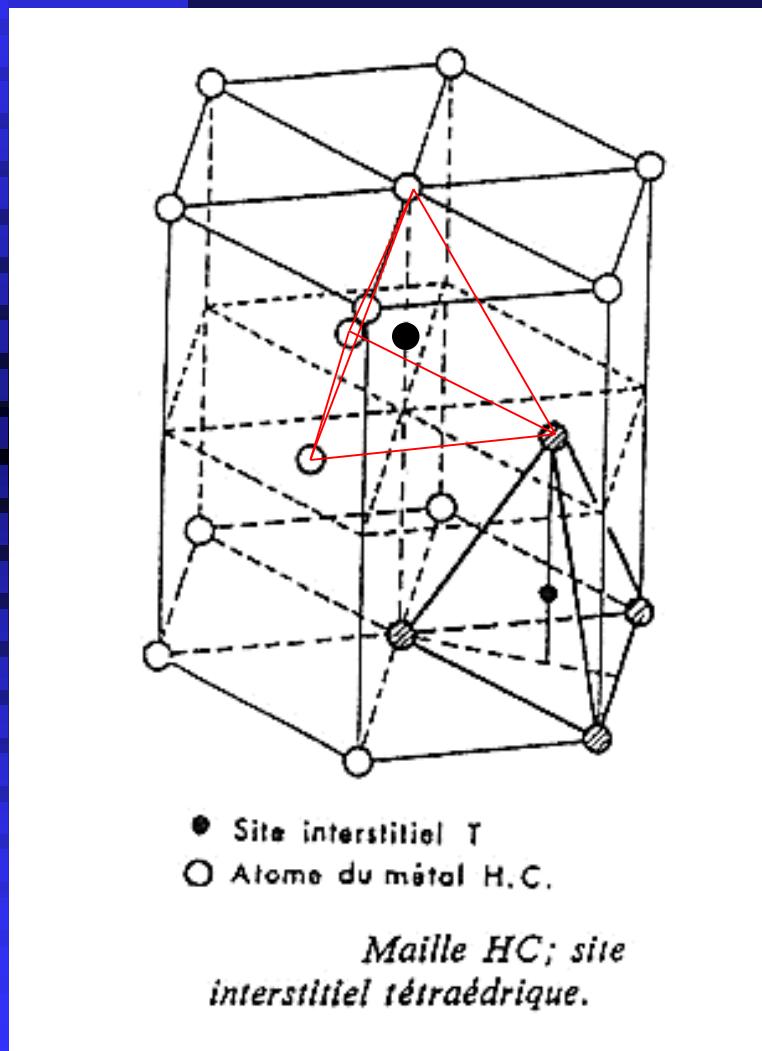


Intersticios octaédricos  $\Rightarrow$  6 huecos/celda

# HC. Huecos octaédricos: $r_i/r_s$

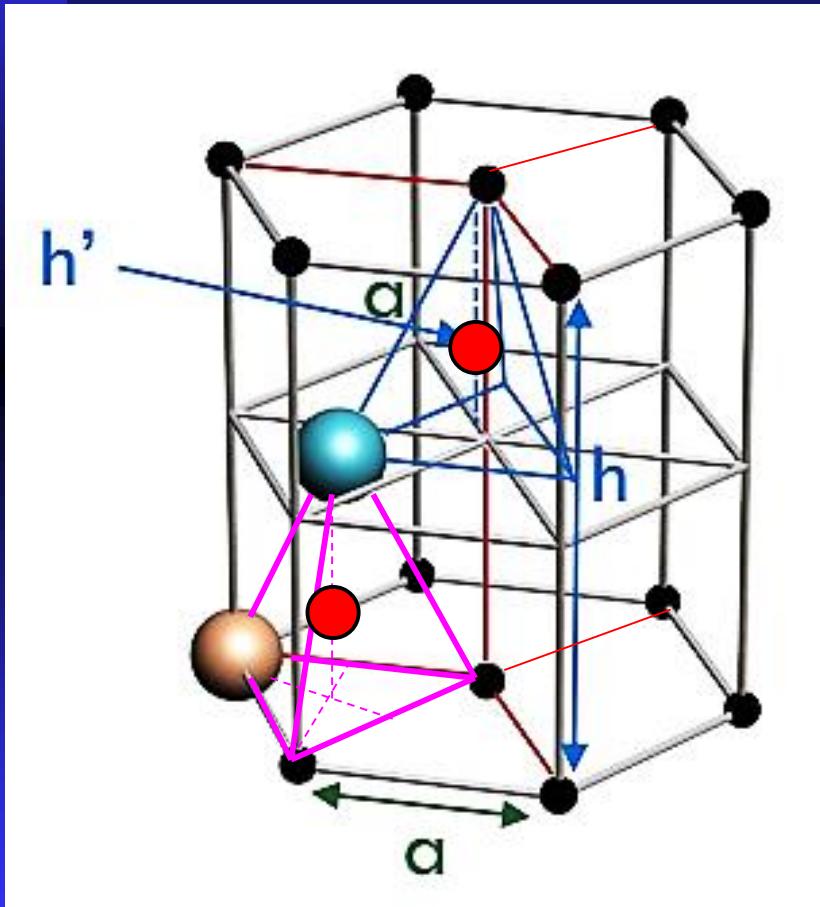


# SISTEMA HC: Huecos tetraédricos



Intersticios tetraédricos: 12 huecos/celda

# SISTEMA HC: Huecos tetraédricos



- ❖ **6 huecos/celda** con tetraedros de las bases.
- ❖ **2 huecos/celda** con tetraedros centrales.
- ❖ **(12/3) huecos/celda** de las aristas
- ❖ **12 ATOMOS/CELDA**

# HC. Huecos tetraédricos: $r_i/r_s$

